

Second-order predicates: assert/1 and retract/1

Powerful: enable run-time program modification

Harmful: code hard to understand and debug, often slow

sometimes used as global variables, "boolean" flags or to memoize:

```
fib(0,0).  
fib(1,1).  
fib(N,F) :-  
    N > 1,  
    N1 is N-1,  
    N2 is N1-1,  
    fib(N1,F1),  
    fib(N2,F2),  
    F is F1+F2.
```

```
mfib(N, F):- memo_fib(N, F), !.  
mfib(N, F):-  
    N > 1,  
    N1 is N-1,  
    N2 is N1-1,  
    mfib(N1,F1),  
    mfib(N2,F2),  
    F is F1+F2,  
    assert(memo_fib(N, F)).  
  
:- dynamic memo_fib/2.  
memo_fib(0,0).  
memo_fib(1,1).
```

if you've remembered an answer for this goal before, return it

most Prologs require such a declaration for clauses that are added or removed from the program at run-time

Higher-order programming using call/N: call(Goal,...)

a more flexible form of call/1, which takes additional arguments that will be added to the Goal that is called

```
call(p(x1,x2,x3))  
call(p(x1,x2), x3)  
call(p(x1), x2, x3)  
call(p, x1, x2, x3)
```

all result in `p(x1, x2, x3)` being called

Supported by most Prolog systems in addition to call/1
can often be used in places where you would use univ operator =.. to construct the goal

Higher-order programming using call/N: implementing map and friends

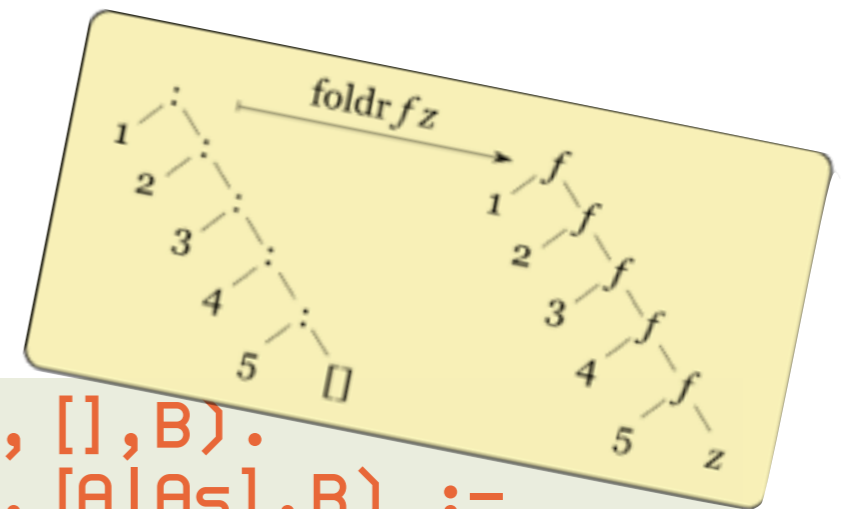
[Higher-order logic programming in Prolog, Lee Naish, 1996]

```
map(_F, [], []).  
map(F, [A0|As0], [A|As]) :-  
  call(F, A0, A),  
  map(F, As0, As).
```

```
filter(_P, [], []).  
filter(P, [A0|As0], As) :-  
  (call(P, A0) ->  
    As = [A0|As1]  
  ; As = As1),  
  filter(P, As0, As1)
```

```
foldr(F, B, [], B).  
foldr(F, B, [A|As], R) :-  
  foldr(F, B, As, R1),  
  call(F, A, R1, R).
```

```
compose(F, G, X, FGX) :-  
  call(G, X, GX),  
  call(F, GX, FGX).
```



Higher-order programming using call/N: using map and friends (1)

[Higher-order logic programming in Prolog, Lee Naish, 1996]

```
?- filter(>(5), [3,4,5,6,7], As).  
As= [3,4]
```

called goal: $>(5,X)$

```
?- map(plus(1), [2,3,4], As).  
As= [3,4,5]
```

```
?- map(between(1), [2,3], As).  
As= [1,1]; As= [1,2]; As= [1,3];  
As= [2,1]; As= [2,2]; As= [2,3]
```

between(I,J,X) binds X to an integer between I and J inclusive.

```
?- map(plus(1), As, [3,4,5]).  
As= [2,3,4]
```

assuming that plus/3 is reversible (e.g., Peano arithmetic)

```
?- map(plus(X), [2,3,4], [3,4,5]).  
X=1
```

```
?- map(plus(X), [2,A,4], [3,4,B]).  
X=1, A=3, B=5
```

relies on execution order in which X is bound first

Higher-order programming using call/N: using map and friends (2)

flatten defined in terms of foldr
using empty list and append

```
?- foldr(append, [], [[2], [3,4], [5]], As).  
As= [2,3,4,5]
```

```
?- compose(map(plus(1)), foldr(append, []), [[2], [3,4], [5]], As).  
As= [3,4,5,6]
```

flattens first, then adds 1

plain Prolog lacks "currying" for higher-order programming:
functional programming languages would return a list of
functions that take the missing argument

conceptual difficulty: ok to curry a call(sum(2,3)) to a sum(2,3,Z)
if there is also a definition for sum(X,Y)?

```
?- map(plus, [2, 3, 4], As).  
ERROR: map/3: Undefined procedure: plus/2  
ERROR:         However, there are definitions for:  
ERROR:         plus/3
```

Inspecting terms: var/1 and its use in practice

var(Term)

succeeds when Term is an uninstantiated variable
nonvar(Term) has opposite behavior

```
?- var(X).  
true.  
?- X=3, var(X).  
false.
```

```
plus(X,Y,Z) :-  
    nonvar(X), nonvar(Y), Z is X+Y.  
plus(X,Y,Z) :-  
    nonvar(X), nonvar(Z), Y is Z-X.  
plus(X,Y,Z) :-  
    nonvar(Y), nonvar(Z), X is Z-Y.
```

ensuring relational
nature of predicates

```
grandparent(X,Z) :-  
    nonvar(X), parent(X,Y), parent(Y,Z).  
grandparent(X,Z) :-  
    nonvar(Z), parent(Y,Z), parent(X,Y).
```

directing search for
efficiency

Inspecting terms: arg/3 and functor/3

complement =..
operator

`arg(N,Term,Arg)`

succeeds when `Arg` is the `N`th argument of `Term`

`functor(Term,F,N)`

succeeds when the `Term` starts with the functor `F` of arity `N`

tests whether a term is ground (i.e., contains no uninstantiated variables)

```
ground(Term) :-  
    nonvar(Term), constant(Term).  
ground(Term) :-  
    nonvar(Term),  
    compound(Term),  
    functor(Term,F,N),  
    ground(N,Term).  
ground(N,Term) :-  
    N > 0,  
    arg(N,Term,Arg),  
    ground(Arg),  
    N1 is N-1,  
    ground(N1,Term).  
ground(0,Term).
```

common Prolog
practice: arity of
auxiliary and main
predicates differ

Extending Prolog: `term_expansion(+In,-Out)`

called by Prolog for
each file it compiles

clause or list of clauses that will be added to
the program instead of the In clause

useful for generation code, e.g. :

given compound term representation of data

```
student(Name, Id)
```

want to use accessor predicates

```
student_name(student(Name, _), Name).  
student_id(student(_, Id), Id).
```

instead of explicit unifications throughout the code

```
Student = student(Name, _)
```

to ensure independence of one particular representation of the data

Extending Prolog: term_expansion(+In,-Out)

```
:- struct student(name,id).
```



```
student_name(student(Name, _), Name).  
student_id(student(_, Id), Id).
```

declares struct as a prefix operator

```
:- op(1150, fx, (struct)).
```

```
term_expansion([:- struct Term), Clauses) :-  
    functor(Term, Name, Arity),  
    functor(Template, Name, Arity),  
    gen_clauses(Arity, Name, Term, Template, Clauses).
```

create Template with same functor and arity, but with variable arguments rather than constants

Extending Prolog: term_expansion(+In,-Out)

N-th argument
recursed upon

```
gen_clauses(N, Name, Term, Template, Clauses) :-  
  (N == 0 ->  
    Clauses = []  
  ;arg(N, Term, Argname),  
  arg(N, Template, Arg),  
  atom_codes(Argname, Argcodes),  
  atom_codes(Name, Namecodes),  
  append(Namecodes, [0'_|Argcodes], Codes),  
  atom_codes(Pred, Codes),  
  Clause =.. [Pred, Template, Arg],  
  Clauses = [Clause|Clauses1],  
  N1 is N - 1,  
  gen_clauses(N1, Name, Term, Template, Clauses1)  
  ).
```

trick to merge
recursive and
base clause

conversion from
atom to list of
character codes

creates fact

When trying out, put gen_clauses/5
before term_expansion/2

```
?- X=0'_.  
X = 95.  
?- char_code(X, 95).  
X = ' '.
```

Extending Prolog: operators

Certain functors and predicate symbols that be used in infix, prefix, or postfix rather than term notation.

```
:- op(500,xfx,'has_color').  
a has_color red.  
b has_color blue.
```

```
?- b has_color C.  
C = blue.  
?- What has_color red.  
What = a
```

integer between 1 and 1200;
smaller integer binds stronger
 $a+b/c \equiv a+(b/c) \equiv +(a,/(b,c))$ if / smaller than +

```
:- op(Precedence, Type, Name)
```

prefix: fx, fy
infix: xfx, xfy, yfx
postfix: xf, yf

associative	not	right	left
	xfx	xfy	yfx
X op Y op Z	/	op(X,op(Y,Z))	op(op(X,Y),Z)

Extending Prolog: operators in towers of Hanoi

```

:- op(900,xfx,to).
hanoi(0,A,B,C,[]).
hanoi(N,A,B,C,Moves):-
    N1 is N-1,
    hanoi(N1,A,C,B,Moves1),
    hanoi(N1,B,A,C,Moves2),
    append(Moves1,[A to C|Moves2],Moves).

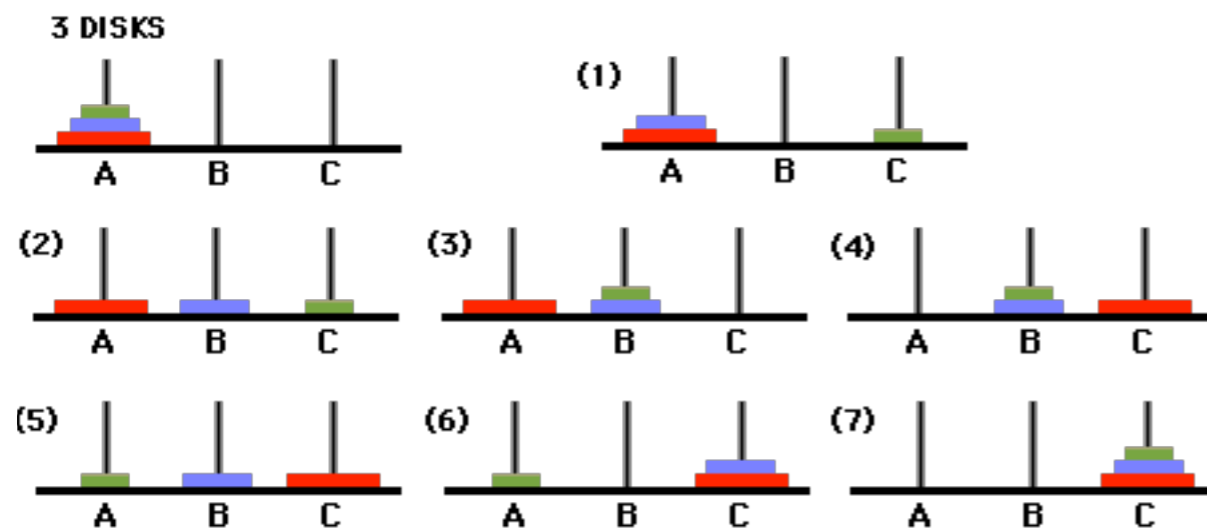
```

Moves is the list of moves to move N discs from peg A to peg C, using peg B as an intermediary.

move n-1 c from A to B.
disc #n is left on A

move n-1 discs from B to C.
they will rest on disc #n

move disc #n from A to C



```

?- hanoi(3,left,middle,right,M)
M = [left to right,
left to middle,
right to middle,
left to right,
middle to left,
middle to right,
left to right ]

```

Extending Prolog: built-in operators

```
1200 xfx -->, :-  
1200 fx  :-, ?-  
1150 fx  dynamic, discontinuous, initialization, meta_predicate, module_  
1100 xfy ;, |  
1050 xfy ->, op*->  
1000 xfy ,  
900 fy  \+  
900 fx  -  
700 xfx <, =, =.., =@=, =:=, =<=, ==, =\=, >, >=, @<, @=<, @>, @>=, \=, \==, is  
600 xfy :  
500 yfx +, -, /\, \/, xor  
500 fx  ?  
400 yfx *, /, //, rdiv, <<, >>, mod, rem  
200 xfx **  
200 xfy ^  
200 fy  +, -, \
```

<code>+(a, /(b,c))</code>	<code>a+b/c</code>
<code>is(X, mod(34, 7))</code>	<code>X is 34 mod 7</code>
<code><('+(3,4),8)</code>	<code>3+4<8</code>
<code>'=(X, f(Y))</code>	<code>X=f(Y)</code>
<code>'-(3)</code>	<code>-3</code>
<code>':-'(p(X), q(Y))</code>	<code>p(X) :- q(Y)</code>
<code>':-'(p(X), ', '(q(Y), r(Z)))</code>	<code>p(X) :- q(Y), r(Z)</code>



clauses are also Prolog terms!

Extending Prolog: vanilla and canonical naf meta-interpreter

```
prove(Goal) :-  
  clause(Goal, Body),  
  prove(Body).  
  
prove((Goal1, Goal2)) :-  
  prove(Goal1),  
  prove(Goal2).  
  
prove(true).
```

Are these meta-circular
interpreters?

```
prove(true) :- !.  
  
prove((A, B)) :- !,  
  prove(A),  
  prove(B).  
  
prove(not(Goal)) :- !,  
  not(prove(Goal)).  
  
prove(A) :-  
  % not (A=true; A=(X,Y); A=not(G))  
  clause(A, B),  
  prove(B).
```

Avoids problems where
clause/2 is called with a
conjunction or true.

clause(:Head, ?Body)

True if *Head* can be unified with a clause head and *Body* with the corresponding clause body. Gives alternative clauses on backtracking. For facts *Body* is unified with the atom *true*.

Availability: built-in
[ISO]

Extending Prolog: meta-level vs object-level in meta-interpreter

	KNOWLEDGE	REASONING
META-LEVEL	<pre>clause(p(X), q(X)). clause(q(a), true).</pre>	<pre>?-prove(p(X)). X=a</pre>
OBJECT-LEVEL	<pre>p(X) :- q(X). q(a).</pre>	<pre>?-p(X). X=a</pre>

Canonical meta-interpreter still **absorbs** backtracking, unification and variable environments implicitly from the object-level.

Reified unification explicit at meta-level :

```
prove(A) :-  
  clause(Head, Body),  
  unify(A, Head, MGU, Result),  
  apply(Body, MGU, NewBody),  
  prove_var(NewBody).
```

Prolog programming:

(might not work equally well for everyone)

a methodology illustrated on partition/4

1 Write down declarative specification

```
% partition(L,N,Littles,Bigs) ← Littles contains numbers
%                               in L smaller than N,
%                               Bigs contains the rest
```

2 Identify recursion and “output” arguments

what is the recursion argument?
what is the base case?

3 Write down implementation skeleton

```
partition([],N,[],[]).
partition([Head|Tail],N,?Littles,?Bigs):-
    /* do something with Head */
    partition(Tail,N,Littles,Bigs).
```

Empty list is partitioned into two empty lists.

We recurse on the “input” argument list.

Prolog programming: a methodology illustrated on partition/4

4 Complete bodies of clauses

```
partition([],N, [], []).  
partition([Head|Tail],N, ?Littles, ?Bigs) :-  
    Head < N,  
    partition(Tail,N,Littles,Bigs),  
    ?Littles = [Head|Littles], ?Bigs = Bigs.  
partition([Head|Tail],N, ?Littles, ?Bigs) :-  
    Head >= N,  
    partition(Tail,N,Littles,Bigs),  
    ?Littles = Littles, ?Bigs = [Head|Bigs].
```

Head is smaller, has to
be added to Littles

has to be added to
Bigs otherwise

5 Fill in "output" arguments

```
partition([],N, [], []).  
partition([Head|Tail],N, [Head|Littles], Bigs) :-  
    Head < N,  
    partition(Tail,N,Littles,Bigs).  
partition([Head|Tail],N, Littles, [Head|Bigs]) :-  
    Head >= N,  
    partition(Tail,N,Littles,Bigs).
```

Prolog programming: a methodology illustrated on sort/2

1 Write down declarative specification

```
⊗ sort(L,S) ← S is a sorted permutation of list L
```

2 Identify recursion and “output” arguments

3 Write down implementation skeleton

```
sort([], []).  
sort([Head|Tail], ?Sorted):-  
    /* do something with Head */  
    sort(Tail, Sorted).
```

4 Complete bodies of clauses

```
sort([], []).  
sort([Head|Tail], WholeSorted):-  
    sort(Tail, Sorted),  
    insert(Head, Sorted, WholeSorted).
```

Auxiliary
predicate

Prolog programming: a methodology illustrated on insert/3

1 Write down declarative specification

```
⌘ insert(X, In, Out) ← In is a sorted list, Out is In  
⌘                       with X inserted in the proper place
```

2 Identify recursion and “output” arguments

3 Write down implementation skeleton

```
insert(X, [], ?Inserted).  
insert(X, [Head|Tail], ?Inserted) :-  
    /* do something with Head */  
    insert(X, Tail, Inserted).
```

Prolog programming: a methodology illustrated on insert/3

4 Complete bodies of clauses

```
insert(X, [], ?Inserted) :-  
    ?Inserted = [X].  
insert(X, [Head|Tail], ?Inserted) :-  
    X > Head,  
    insert(X, Tail, Inserted),  
    ?Inserted = [Head|Inserted].  
insert(X, [Head|Tail], ?Inserted) :-  
    X <= Head,  
    ?Inserted = [X, Head|Tail].
```

5 Fill in "output" arguments

```
insert(X, [], [X]).  
insert(X, [Head|Tail], [X, Head|Tail]) :-  
    X <= Head.  
insert(X, [Head|Tail], [Head|Inserted]) :-  
    X > Head,  
    insert(X, Tail, Inserted).
```

More Prolog programming: quicksort

```
quicksort([], []).
quicksort([X|Xs], Sorted) :-
    partition(Xs, X, Littles, Bigs),
    quicksort(Littles, SortedLittles),
    quicksort(Bigs, SortedBigs),
    append(SortedLittles, [X|SortedBigs], Sorted).
```

with difference lists:

```
quicksort(Xs, Ys) :- qsort(Xs, Ys-[]).

qsort([], Ys-Ys).
qsort([X0|Xs], Ys-Zs) :-
    partition(Xs, X0, Ls, Bs),
    qsort(Bs, Ys2-Zs),
    qsort(Ls, Ys-[X0|Ys2]).
```